

London Taught Course Centre

2010 Examination

Algebraic Topology

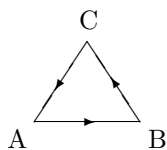
*Answer both questions*

1. Explain why the simplicial homology of a  $\Delta$ -complex  $K$  is independent of the particular subdivision used to compute it.

2.  $ABC$  is a triangle.  $AB$ ,  $BC$ ,  $CA$  are identified (glued) in the directions shown, the resulting space being called  $Y$ .

Give reasons why a)  $Y$  is not a surface and b) it contains a Möbius band.

Find a way of expressing  $Y$  as a  $\Delta$ -complex, and find its simplicial homology groups.



*Luke Hodgkin, April 2010*