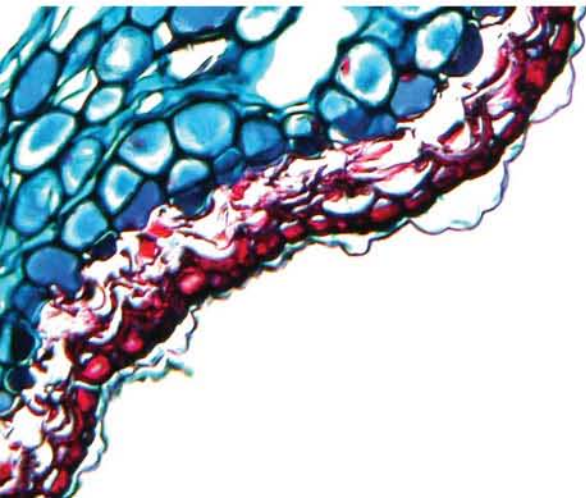


Imperial College LTTC Course  
10MAR2010  
Andy Garrett

*A personal view on how statistics is used in practice  
in the pharmaceutical industry*



clinical | commercial | consulting | capital

# Content

- History of statistics in drug development and some basic concepts
- How to get into the profession
- Some simple illustrations of problems faced
- Two examples
  - Logistics regression, covariate adjustment and non-inferiority
  - Simpson's paradox
  - RSS First in Man WP
- Current areas of statistics research in the industry

# History of drug regulation

- Drug regulation driven primarily from US, but now International (ICH, 1991)
- 1906 Pure Food and Drug Act response to concerns adulteration and misbranding of food and drugs - focus was drug labelling not drug approval
- 1938 Food, Drug and Cosmetic Act required regulatory approval prior to marketing – proof of safety
- 1962 Kefauver-Harris Amendments added proof of efficacy
  - Requirement to submit *substantial evidence* to support regulatory approval and for this to originate from *adequate and well-controlled investigations*.
  - defining moment for statistics in drug development, made sound statistical methodology an integral part of the regulatory process
- Regulation as responses to notable tragic events - such as thalidomide related birth defects (1962 K-H Amendments) - or to growing concerns regarding activities – e.g. reluctance to conduct paediatric studies (2002 Best Pharmaceuticals for Children Act).

# How do get into the profession

## – Global

- Travel, TCs! India, China

## – Teamwork

- Communication
- Organised

## – Masters / PhD

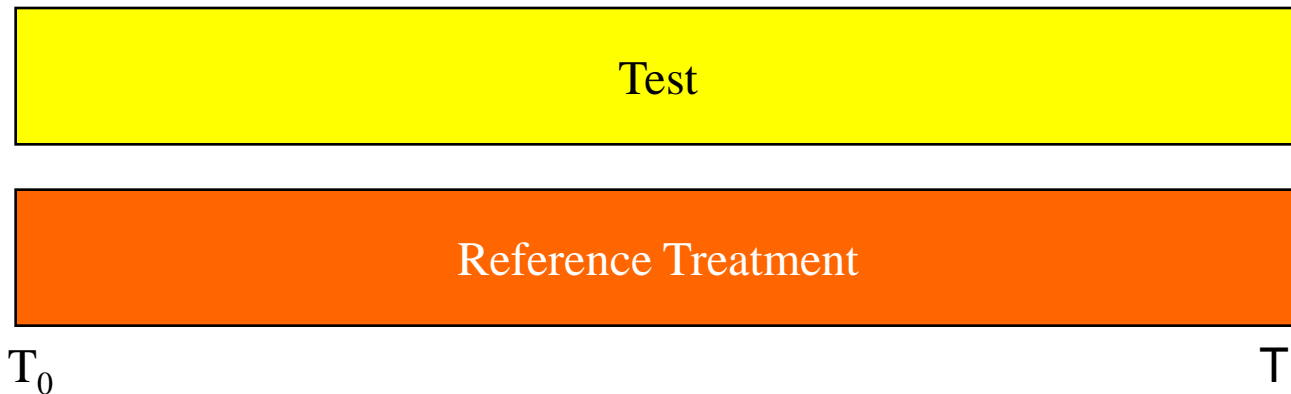
- Continuing professional development

– Pharmaceutical / biotech

– CROs (Pharmaceutical Services) – e.g. Quintiles

– Academic/Research – e.g. MRC

# Basic randomised, controlled trial



## Randomisation

- RA Fisher developed randomised experimentation with Bradford Hill applying to clinical research in the 1950's
- Over all randomisations, treatment groups will be balanced with respect to both known & unknown factors that influence outcome.
- If exclude patients may introduce bias (Intent to treat principle)
- Estimate the treatment difference at  $T_1$ , construct CI to give range of plausible values. Most likely this will involve modelling (covariate adjustment)

## Some simple illustrations – because they have an impact!

- Change from BL
- % change from BL
- Dichotomisation of endpoints

Senn & Julious (2009)

# Use of baseline to construct change scores

Change scored is  $D = Y - X$

where  $Y$  is outcome variable and  $X$  is the same variable at baseline

T-test to compare two treatments ( $T$ ) is essentially

$$(Y - X) = \alpha + \beta_2 T$$

Re-arrange to get

$$Y = \alpha + X + \beta_2 T$$

ANCOVA is generally more efficient (i.e. more powerful)

$$Y = \alpha + \beta_1 X + \beta_2 T \quad (\text{In t-test, forcing } \beta_1 = 1)$$

Often one sees Change from baseline, with baseline as a covariate

$$(Y - X) = \alpha + \beta_3 X + \beta_2 T$$

$$Y = \alpha + (\beta_3 + 1) X + \beta_2 T \quad (\text{Identical parametrisation of treatment, but } \beta_1 = (\beta_3 + 1))$$

Key point is that baseline should be fitted as a covariate since the relative efficiency of  $(Y-X)$  versus ANCOVA is  $(1 + \rho)/2$ , where  $\rho$  is the correlation between  $Y$  and  $X$

## Percentage change from baseline

$$100 \times (Y - X) / X$$

Same as  $100 \times (Y/X - 1)$ , so working part is simply  $Y/X$

Ratio unlikely to be normal, even if  $Y$  and  $X$  are normal

- Tends to be more of an issue when  $X$  is small and changes are large
- Data will be approx Normal if means are large compared to SD

Ratio are not good candidates for parametric analysis therefore

Typically take Logs instead

$$\text{Log}(Y) = \alpha + \beta_1 \log(X) + \beta_2 T$$

Note cannot take logs of negative numbers or zero

Key point: do not analyse data as percentage change from baseline



# The loss in creating artificial dichotomies

Dichotomisation of normal data

Pitman efficiency of sign-test versus t-test is  $(2/\pi) \approx 64\%$

- Assumes median split
- E.g. if abnormal is 2 SD from mean then relative efficiency is only 13%

Key finding: analyse on continuous scale but use dichotomisation to aid interpretation

If dichotomy is used then it is not possible to recover the full information provided by baseline (double whammy!)

A more detailed example – logistic regression, covariate adjustment & non-inferiority

# Stratified binary data example (Balanced 2x2x2 table)

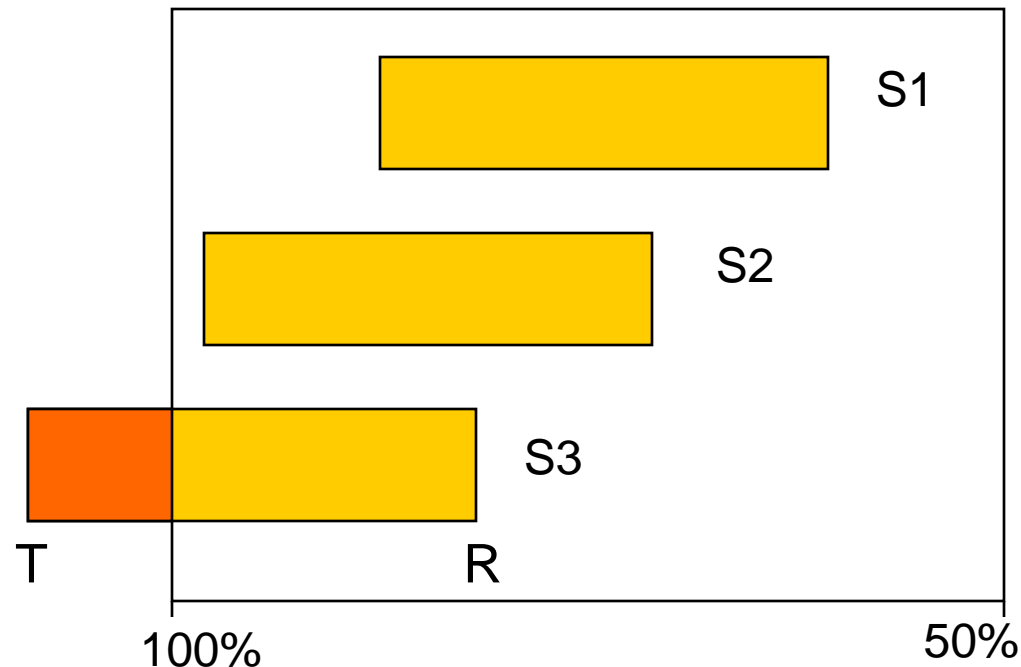


|           | Males<br>Diff=15%<br>OR=3                | Females<br>Diff=25%<br>OR=3            | Total<br>Diff=20%<br>OR=2.83                  |
|-----------|--|--|---|
| Test      | <b>90/100 = 90%</b><br>odds 90/10<br>= 9 | <b>75/100=75%</b><br>odds 75/25<br>= 3 | <b>165/200=82.5%</b><br>odds 165/35<br>= 4.71 |
| Reference | <b>75/100 =75%</b><br>odds 75/25<br>= 3  | <b>50/100=50%</b><br>odds 50/50<br>= 1 | <b>125/200=62.5%</b><br>odds 125/75<br>= 1.67 |

# Basic principles: stratified analyses

- Choose scale of measurement
- Stratified model
  - Primary model, if stratified design (analyse as you design)
  - Estimate adjusted treatment difference
    - Estimate each *within stratum* treatment difference
    - Combine these estimates using a system of weights
  - Confidence interval
  - Significance test (p-value)
- Investigation of consistency of effect
  - treatment by factor interaction

# Difference in Percentages



In stratum S3, the Reference response is too high such that the treatment difference cannot be consistent with those observed in strata S1 & S2

See Smith *et al* (1998) for stratified analyses for the difference in proportions. Also Koch & Carr (1990)

## Logistic model

- Models the  $\log_e$  (odds)
- $\beta$  is a  $\log_e$  (odds ratio)
- It follows that  $e^\beta$  is an odds ratio

$$\ln(odds) = \ln\left(\frac{\pi}{1-\pi}\right) = \alpha + \beta_1 \cdot strata + \beta_2 \cdot treatment$$

# Main effects model



$$\begin{bmatrix} \ln(odds_{1r}) \\ \ln(odds_{1t}) \\ \ln(odds_{2r}) \\ \ln(odds_{2t}) \end{bmatrix} = \begin{bmatrix} \alpha \\ \alpha \\ \alpha + \beta_1 \\ \alpha + \beta_1 + \beta_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta_1 \\ \beta_2 \end{bmatrix}$$

Log odds for  
reference cell

Increment for log odds for  
test treatment - that is,  
 $\ln(\text{OR})$

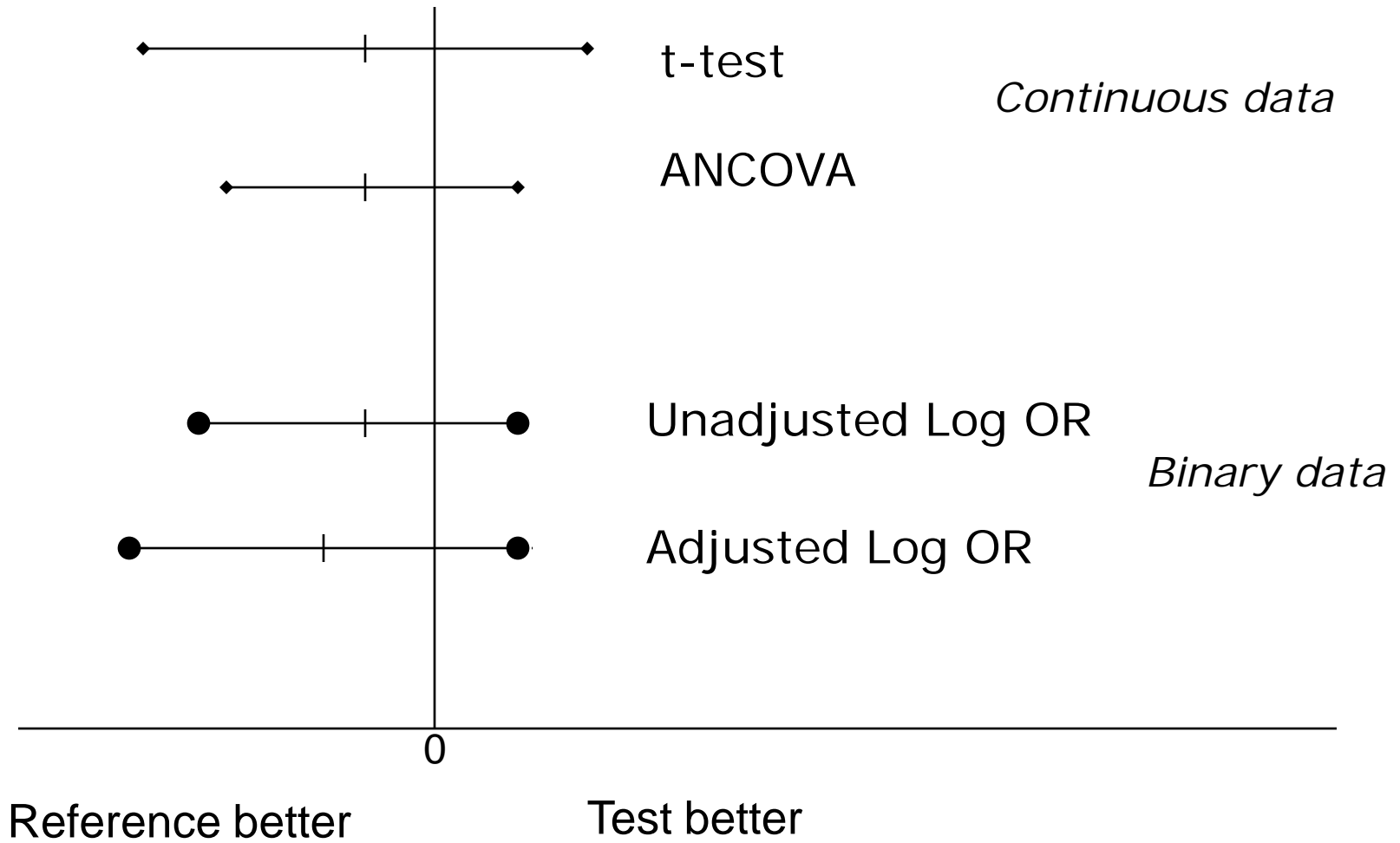
Design matrix

## Covariate adjustment

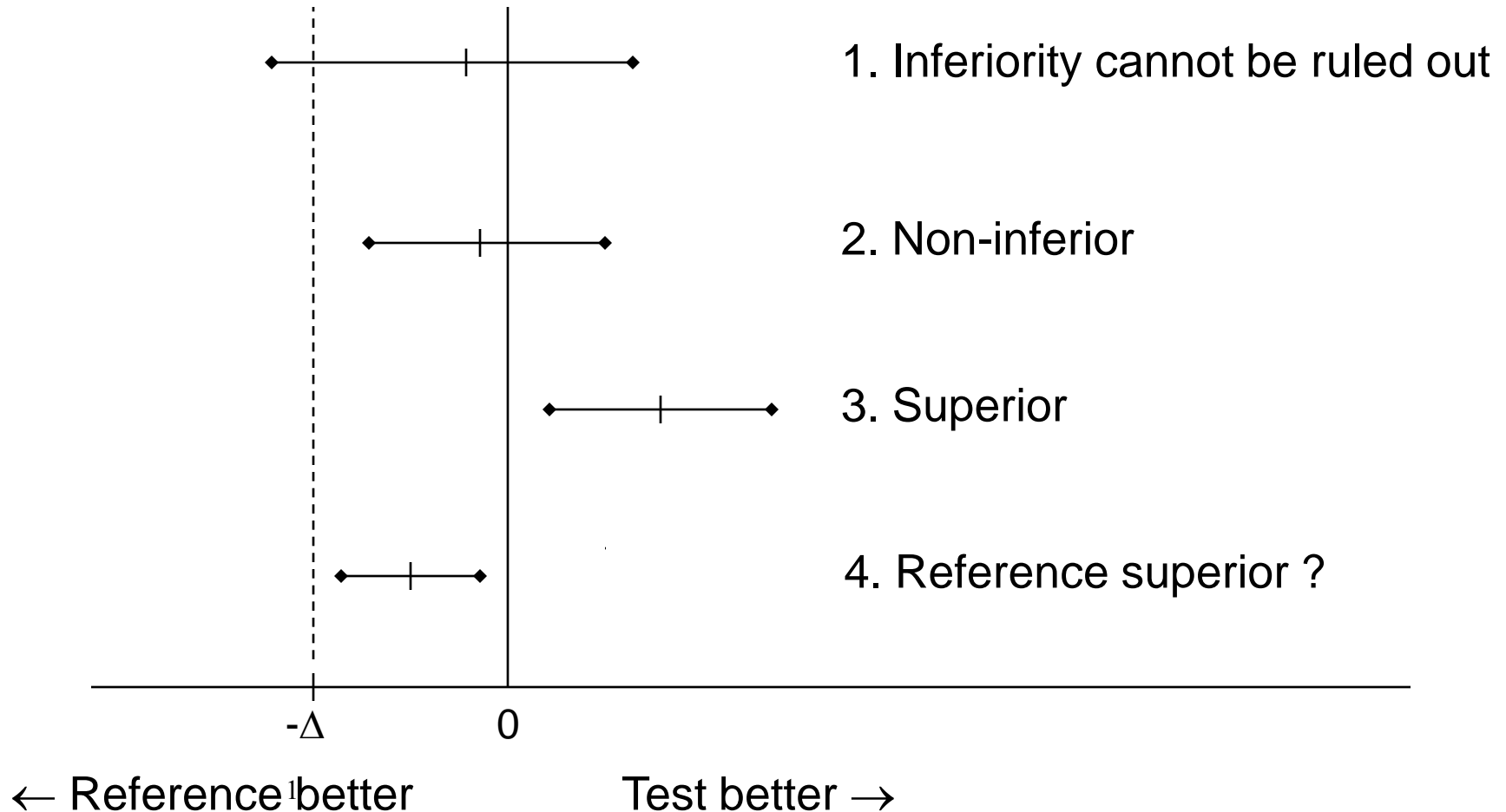
- If a factor exists which independently affects outcome then **excluding** this factor from the logistic model leads to:
  - underestimation of a non unity treatment difference
  - an increase in precision for the estimated treatment difference
- Combined effect of including a factor is an increase in efficiency - strategy of covariate adjustment justified for superiority - but what about non-inferiority
- Robinson *et al* (1991, 1998)



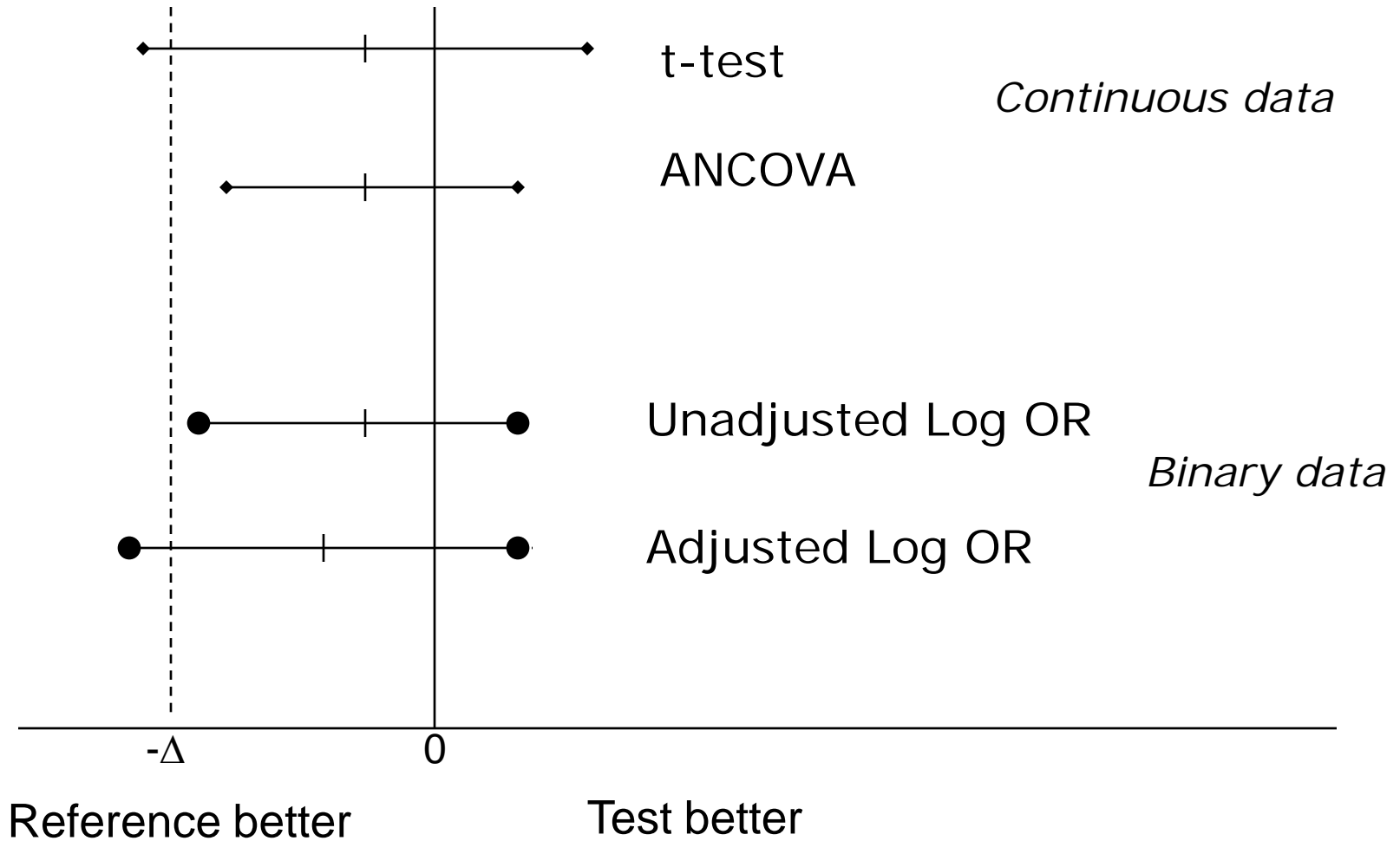
# Impact of factor adjustment on Log OR & SE



# Non-inferiority



# Impact of factor adjustment on Log OR & SE: Effect on NI trials



## Simulation (logistic model)

| $\psi_F$ | Model      | % non inferior   |              |
|----------|------------|------------------|--------------|
|          |            | $\psi_T = 0.538$ | $\psi_T = 1$ |
| 1        | T          | 2.74             | 82.10        |
|          | F+T        | 2.58             | 81.94        |
| 2        | T          | 2.80             | 81.14        |
|          | F+T        | 2.20             | 79.98        |
| 3        | T          | 3.62             | 82.78        |
|          | F+T        | 2.52             | 79.86        |
| 4        | <b>T</b>   | <b>5.02</b>      | <b>82.32</b> |
|          | <b>F+T</b> | <b>2.78</b>      | <b>76.52</b> |

N=5000 simulations with sample size of 175 per treatment to show non-inferiority within 15% of a Reference percentage of 50% (one sided type I error of 2.5%, 80% power). F is a two level factor (Garrett, 2003)

# IMPACT: NI, logistic & covariate adjustment

- When the factor effect is large then the type I error is approximately doubled if the factor is excluded
  - type I error: conclude non-inferiority when really inferior
- However unadjusted model has greater power - since when there is no treatment difference, covariate adjustment increases the SE.
  - Power: conclude non-inferiority when really non-inferior

# Simpson's Paradox

Historical comparison of kidney stone removal  
(Charig et al, 1986)



|             | <2 cm<br>Diff= +6%<br>OR=2.1   | >=2 cm<br>Diff= +4%<br>OR=1.2  | Total<br>Diff= -5%<br>OR=0.7   |
|-------------|--------------------------------|--------------------------------|--------------------------------|
| OS, 1972-80 | <b>81/87=93%</b><br>odds =13.5 | <b>192/263=73%</b><br>odds=2.7 | <b>273/350=78%</b><br>odds=3.5 |
| PN, 1980-85 | <b>234/270=87%</b><br>odds=6.5 | <b>55/80= 69%</b><br>odds=2.2  | <b>289/350=83%</b><br>odds=4.7 |

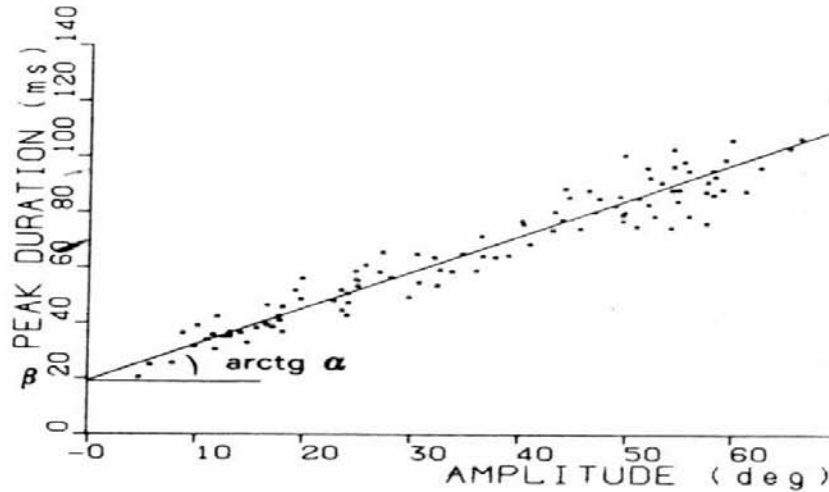
Percutaneous nephrolithotomy (PN) vs. open surgery (OS) by stone diameter

# Actual RCT example: Gaucher's disease: SEMV parameter estimation

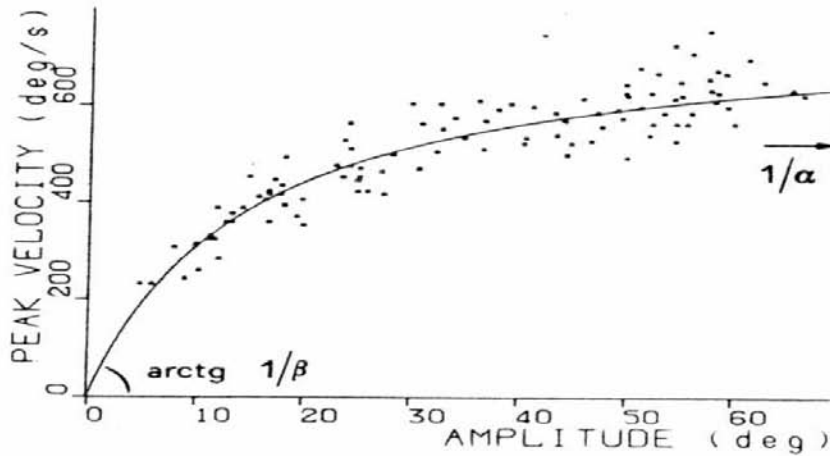


↓ slope ( $\alpha$ ) = improvement

↓ intercept ( $\beta$ ) = improvement



(a)



(b)

↑  $1/\alpha$  = improvement

↑  $1/\beta$  = improvement



|         | Centre 1<br>Diff <b>-0.869</b> | Centre 2<br>Diff <b>-0.284</b> | Total<br>Diff <b>0.190</b> |
|---------|--------------------------------|--------------------------------|----------------------------|
| Test    | <b>0.554</b><br>(14)           | <b>-0.534</b><br>(4)           | <b>0.312</b><br>(18)       |
| Control | <b>1.423</b><br>(2)            | <b>-0.250</b><br>(7)           | <b>0.122</b><br>(9)        |

- 30 patients enrolled in RCT with 2:1 randomisation (active : placebo)
- Primary endpoint saccadic eye movement (quantitative endpoint)
- Mean change in slope  $\alpha$  from BL to M12
- Study not stratified by centre as open-label design (avoid selection bias) led to some imbalance – exaggerated by:
  1. One patient refused Test, and followed as if Control
  2. Two patients in Test group and one in Control group with no saccade data



## RSS First in man WP (TGN1412 study)

- A monoclonal antibody (rheumatoid arthritis, leukaemia etc)
- First-in-man study (13MAR06) conducted by Parexel on behalf of TeGenero
- In first cohort 8 volunteers
  - Six allocated TGN1412 and two allocated placebo
- All six given TGN1412 suffered a cytokine storm and by that evening had been admitted to intensive care



*worst affected,  
suffering heart, liver  
and kidney failure,  
pneumonia, and  
septicaemia.*

## Study Outcome in a Conventional Format

|           |              | Adverse Reaction? |     |       |
|-----------|--------------|-------------------|-----|-------|
|           |              | No                | Yes | Total |
| Treatment | Placebo      | 2                 | 0   | 2     |
|           | TGN 1412     | 0                 | 6   | 6     |
|           | <b>Total</b> | 2                 | 6   | 8     |

**Table 1.** Fourfold summary showing healthy volunteers cross-classified by treatment and outcome.

| Step | TGN1412                  |                       | Placebo               |
|------|--------------------------|-----------------------|-----------------------|
|      | Dose Mg/Kg<br>bodyweight | Number of<br>Subjects | Number of<br>Subjects |
| 1    | 0.1                      | 6                     | 2                     |
| 2    | 0.5                      | 6                     | 2                     |
| 3    | 2.0                      | 6                     | 2                     |
| 4    | 5.0                      | 6                     | 2                     |

Table 1: Design given in the protocol

## Questions

1. Why 6 + 2
2. Why four doses?
3. Why those dose increases?
4. Why simultaneous treatment in cohorts?

## Adverse event classification (Strom, 1995):

1. Type A: predictable; dose related; less severe, extension of pharmacological effect
2. Type B: unpredictable, severe not related to dose (potentially hypersensitivity, immunological reactions)

## To pool across cohorts or not?

- ‘Yes’, according to the protocol
- But then misleading to describe the trial as double-blind
  
- Bias variance trade-off
  - The proposed analysis would not eliminate the biases blinding is designed to eliminate
- Also what about the analysis at the end of each dose step to guide dose-escalation
- How would this permit pooling of placebo subjects

## Rosemary Bailey's work in Senn (2007)

Bailey recommends designs that follow:

- Halving principle, in which no treatment is allocated to more than half of the subjects
- Diversity principle, where as many different treatments as possible are applied in each cohort
- Extra cohort principle, which means that there should be one more cohort than doses.

| Design | Number of subjects |   |   |   | Variance of differences between doses, and between placebo and each dose, if |   |      |      |  |   |      |      |      |
|--------|--------------------|---|---|---|--|---|------|------|--|---|------|------|------|
|        |                    |   |   |   | a cohort effect is fitted  |   |      |      | it is known that there is no cohort effect |   |      |      |      |
|        | Dose               | 0 | 1 | 2 | 3  |   | 1    | 2    | 3  |   | 1    | 2    | 3    |
| 1      | Cohort 1           | 2 | 6 | 0 | 0  | 0 | 0.67 | 0.67 | 0.67                                       | 0 | 0.33 | 0.33 | 0.33 |
|        | Cohort 2           | 2 | 0 | 6 | 0  | 1 |      | 1.33 | 1.33                                       | 1 |      | 0.33 | 0.33 |
|        | Cohort 3           | 2 | 0 | 0 | 6  | 2 |      |      | 1.33                                       | 2 |      |      | 0.33 |
|        |                    |   |   |   |  |   |      |      |  |   |      |      |      |
| 2      | Cohort 1           | 4 | 4 | 0 | 0  | 0 | 0.50 | 0.50 | 0.50                                       | 0 | 0.33 | 0.33 | 0.33 |
|        | Cohort 2           | 4 | 0 | 4 | 0  | 1 |      | 1.00 | 1.00                                       | 1 |      | 0.50 | 0.50 |
|        | Cohort 3           | 4 | 0 | 0 | 4  | 2 |      |      | 1.00                                       | 2 |      |      | 0.50 |
|        |                    |   |   |   |  |   |      |      |  |   |      |      |      |
| 3      | Cohort 1           | 4 | 4 | 0 | 0  | 0 | 0.29 | 0.40 | 0.65                                       | 0 | 0.29 | 0.31 | 0.39 |
|        | Cohort 2           | 2 | 2 | 4 | 0  | 1 |      | 0.40 | 0.65                                       | 1 |      | 0.31 | 0.39 |
|        | Cohort 3           | 1 | 1 | 2 | 4  | 2 |      |      | 0.58                                       | 2 |      |      | 0.42 |
|        |                    |   |   |   |  |   |      |      |  |   |      |      |      |

## Contrast calculations

– In cohort i (n=6 dose vs n=2 PB):

–  $\text{Var}(\text{dose } i - \text{PB}) = \text{Var}(\text{dose } i) + \text{Var}(\text{PB})$

–  $(1/6 + 1/2) \sigma^2 = 2/3 \sigma^2$

– Ignoring cohort i (n=6 dose vs n=6 PB):

–  $(1/6 + 1/6) \sigma^2 = 2/6 \sigma^2$

## Current areas of statistics research in the industry

Adaptive designs

Missing data

Non-inferiority and relative effectiveness

Bayesian

Analytics/data mining

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