

LTCC COURSE IN DYNAMICAL FUNCTIONAL EQUATIONS AND THEIR APPLICATIONS

- Course Title: Dynamical Functional Equations and their Applications
- Core Audience: First year graduate students and beyond
- Course Format: Extended (10 hours at 2 hours per week)
- Keywords: functional equation, iteration, nonlinear dynamics, renormalization, linearization, Schröder and Abel equations
- Lectures. Five two-hour lectures on the following topics:
 - (1) Overview of elementary concepts from dynamical systems: iteration, fixed points and periodic orbits, stability, conjugacy and semi-conjugacy, fundamental domains. We shall also give a brief overview the most important classical examples of dynamical systems.
 - (2) Dynamical Functional equations: introduction and examples.
 - (3) One dimensional Schröder's equation: properties, solution, applications. Higher dimensional examples: linearization of maps and differential equations around fixed/equilibrium points
 - (4) Abel's equation, properties, solution, and applications. The one-dimensional linear functional equation, including applications to log-periodic power laws in the natural sciences and finance.
 - (5) Linear functional equations, definition, relationship to iterated function systems, spectral and other properties of associated operators. Examples and applications.
 - (6) Nonlinear functional equations, examples including the Feigenbaum functional equation, solution methods, application to critical phenomena in dynamical systems.
- Format
 - (1) Four exercise sheets
 - (2) Electronic notes (to be made available after end of course, if not earlier)
- Prerequisites: Standard undergraduate courses in real and complex analysis and ordinary differential equations. Some knowledge of nonlinear dynamical systems would be an advantage but is not necessary.
- References
 - Jaroslav Smítal, *On Functions and Functional Equations*, Adam Hilger, 1988, ISBN 0852744188. (This is a nice introduction to functional equations.)
 - Marek Kuczma, Bogdan Choczewski, Roman Ger, *Iterative Functional Equations* Issue 32 of *Encyclopedia of Mathematics and its Applications*, ISSN 0953-4806, Cambridge University Press, 1990, ISBN 0521355613, 9780521355612

(This is a comprehensive book on functional equations, suitable for those who wish to take their studies further.)

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